Mode conversion noise attenuation, modelling and removal: case studies from Cyprus and Egypt

Jyoti Kumar1, Marcus Bell1, Mamdouh Salem1, Tony Martin1 and Stuart Fairhead1 propose a method to attenuate converted mode energy to improve the imaging for prospective sub-salt targets.

Introduction
The wavefront from a source that strikes an acoustic impedance contrast separates into four variables: transmitted and reflected compressional waves (P-wave) and transmitted and reflected shear waves (S-wave). Converted waves are those whose mode changes at the interface and can be recorded in a marine environment in the presence of large velocity contrasts. The difference in acoustic velocities at the boundary means that in high contrast media the distinction between compressional and shear velocities across the boundary is small; shear waves are not as refracted as compressional waves and can be recorded as partially converted reflected energy.

The eastern Mediterranean contains two major sedimentary basins, the Levantine and Herodotus (see Figure 1). They have shared depositional regimes and therefore contain similar sedimentary sequences. The Levantine Basin sits offshore Cyprus, Israel, Palestine and Lebanon, and was formed by prolonged phased rifting, with subsequent subsidence and loading by deltaic sediments (Gradmann et al., 2005; Gardosh and Druckman, 2006). It forms a northeast-oriented depression about 2 km deep and contains more than 14 km of Mesozoic and Cenozoic sequences that include up to 2 km of Messinian salt (Druckman et al., 1995; Ben-Avraham et al., 2002; Netzeband et al., 2006). The local reservoirs include both Cretaceous and Jurassic sandstones and limestones, with older potential reservoirs in the Triassic sandstones. Shales and marls of Paleogene, Neogene, Cretaceous and Jurassic, along with Messinian salt and Triassic evaporites all form local seals (Roberts and Peace, 2007) in plays of both stratigraphic and structural nature.

The Herodotus Basin is a northeast trending 3 km deep depression, and represents a slab of the Early Mesozoic Neo-Tethys Ocean (see Figures 1 and 2). The basin is bounded on the north by the Mediterranean Ridge; on the northeast by the west portion of the Cyprus Arc and on the south by the Nile Delta cone. The Eratosthenes Seamount (ESM), a fragment of continental crust (Robertson, 1998), forms the eastern limit of the Herodotus Basin, and additionally delineates the boundary between the cone of the Nile Delta, the Herodotus Basin, and the Levant Basin. The Herodotus Basin itself contains up to 7 km of Mesozoic–Cenozoic sediment (Voogd and Truffer, 1992; Garfunkel, 1998), and is overlain by up to 3 km of Messinian salt (Garfunkel, 1998; Aal et al., 2000; Loncke et al., 2006).

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* Corresponding author, E-mail: jyoti.kumar@pgs.com
amplitude analysis (AVA) of pre-stack data. It can also assist in improving velocity model building (VMB). In this paper we proposed a method to suppress this energy by modelling the converted wave energy using 3D acoustic modelling.

**Method**

**Defining the problem**

Converted mode contamination of P-wave images is a well-known and pernicious problem in some geological settings. In salt provinces, the large velocity contrast between the salt and surrounding sediments generates conversion between P-wave and S-wave energy. This often results in recording of converted mode events. Because the converted mode has a slower apparent velocity, the converted energy occurs deeper than the high contrast boundary and can obscure data interpretability and potential prospectivity. The presence of a Messinian salt layer in this region creates large velocity contrasts between the salt and surrounding sediments. This can generate uncertainty in imaging around potential prospects (Elbassiony et al., 2018). Single value P-wave velocities for the salt in this region are approximately 4200 m/s, whereas the sediment velocity in the post-Messinian overburden and pre-Messinian range from 2400 to 3000 m/s. This strong acoustic velocity contrast at the top and base of salt layer often results in mode conversion. Many prospects in this region are sub-salt, frequently in the vicinity of the recorded converted mode energy. Suppressing this energy has a strong positive impact on the interpretation of potential prospects, particularly in revealing play delineation, but also enabling more accurate
Salt geometries. Dual-leg 3D acoustic modelling has been proposed to model converted wave energy (Huang et al., 2013), which was subsequently used to attenuate it from a pre-migration or post-migration dataset. In the presence of complex salt geometries, diffractions from the top salt interfere with the converted mode generated by the base salt, modelled during forward propagation. This makes it difficult to subtract the converted wave energy before migration. In this paper we perform 3D acoustic modelling twice, with and without the base salt interface in the velocity model used for the propagation. This generates a much cleaner converted wave model that can be subtracted from both pre-stack and pre-migration gathers more effectively.

Solution

The ratio ($r$) between the salt thickness in time ($\Delta t_{salt}$) and the time interval between P-wave and converted-wave base salt ($\Delta t_{csw}$) on time migrated data can be used to identify whether the converted mode has propagated as an S-wave on one or both of the down-going and up-coming wave-fields within the salt.

Existing methods to suppress converted modes include filtering the offending energy based on normal move-out velocity, as converted waves travel with a slower S-wave component (Ogilvie and Purnell, 1996), or surgical muting of energy using travel time ray-tracing (Lu et al., 2003). The effectiveness of both these methods could be significantly reduced in the presence of complex salt geometries. Dual-leg 3D acoustic modelling has been proposed to model converted wave energy (Huang et al., 2013), which was subsequently used to attenuate it from a pre-migration or post-migration dataset. In the presence of complex salt geometries, diffractions from the top salt interfere with the converted mode generated by the base salt, modelled during forward propagation. This makes it difficult to subtract the converted wave energy before migration. In this paper we perform 3D acoustic modelling twice, with and without the base salt interface in the velocity model used for the propagation. This generates a much cleaner converted wave model that can be subtracted from both pre-stack and pre-migration gathers more effectively.

Figure 4 Conceptual overview of the converted wave (C-wave) attenuation methodology.

Figure 5 Different stages of modelling: 3D acoustic forward modelling with the base salt reflector included in the modelling (a); forward modelling without the base salt reflector in the model (b) and a subtraction of the two models (a and b) to generate a clean converted wave model (c).
Assuming zero-offset raypaths, the ratio ($r$) can be expressed mathematically as follows (Lu et al., 2003):

$$ r = \frac{M_{salt}}{M_{cw}} = \frac{\frac{1}{v_p} \frac{1}{v_s}}{\frac{1}{v_p} \frac{1}{v_s} + \frac{1}{v_p}} = 2 \left( \frac{v_s}{v_p} \right) $$ (1)

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The ratio for asymmetrical mode can be calculated using eq (1) and its value is generally between 2 and 3, whereas the ratio for symmetrical mode can be calculated using eq (2). The value of the ratios in this case is significantly lower, between 1 and 1.5. This information aids the selection of the type of converted mode required during the forward modelling process.

The method proposed to suppress the converted mode is presented in Figure 4. The first step in the flow is to obtain a suitable interval velocity model for the P-wave data with an accurate salt layer geometry. Following this, a version of the velocity model containing the S-wave velocity within the salt body is built. The S-wave velocity is obtained by scanning for the velocity that flattens the converted mode energy at the same depth as the interpreted base salt. 3D Finite Difference shot modelling is then performed using a single scattering approximation to produce modelled shot gathers corresponding to the wavefields (PSPP, PPSP and PSSP) resulting from conversion at the top salt and reflection from the base salt reflectors (Figure 5a). It can be clearly observed in Figure 5a that this model is not sufficient as diffractions from the top salt mask the converted mode energy, making it difficult to subtract from the input dataset. An additional 3D finite difference modelling step is performed to model P-waves without any reflection from the base salt reflectors (Figure 5b). A difference is produced of the model obtained from the two forward modelling processes, producing a clean converted mode only model (Figure 5c).

The difference represents the converted wave (C-wave) only model, and is adaptively subtracted from the input shot gather suppressing the recorded PSPP, PPSP and PSSP converted mode energy.

The adaptive subtraction is an important step in the workflow. This is required to compensate for small errors in modelled time and amplitude, which may be owing to either interpretation or errors in the velocity model used for forward modelling step. Intelligent adaptive subtraction (Perrier et al. 2017) was used to subtract the converted wave model from the input dataset. The
and with a total surface spread width covering 1300 m. Two source arrays were used shooting at 25 m flip to flop. The nominal seismic acquisition bin size was 6.25 m by 25 m, with 80 fold of coverage.

The modelling of symmetrical modes (PSSP) was ignored in this case, owing to a lack of evidence of its presence in the recorded field data. The ratio ($r$), described in equations (1) and (2), was estimated at 2.2, inferring that the converted mode was recorded with only one of the up-coming or down-going wave-fields as an S-wave in the salt layer; either PSPP, or PPSP, or both (Figure 5).

The velocity model for the modelling was generated using tomography in the post-salt section to estimate the sediment velocity. The salt layer velocity was estimated using a salt flooding methodology after interpreting the top salt reflection. The aim of this flooding step was to obtain optimal flatness of the base salt reflection. For this dataset, the P-wave velocity of the salt was estimated at 4200 m/s, whereas the S-wave velocity was estimated as 2400 m/s.

The result of the converted wave attenuation workflow is shown in both data and image domains. In Figure 6a, the red arrows clearly indicate the converted wave energy. As expected, the energy has the same phase response as the base salt reflection, but with a delayed recorded time. This is sometimes referred to as the base salt ghost reflection. Figure 6b shows the same technique combines intelligently least square filtering in the time-space domain and a curvelet domain-based subtraction (Nguyen et al. 2017) to adapt the model more effectively. It preserves primary energy, which is absent in the model, by using a ‘true model’ adaptive subtraction technique.

The computed model from the first forward modelling step can be used to suppress the converted mode directly, but in this case the subtraction has to be done in the image domain where diffractions from the top-salt have collapsed and do not to mask the converted wave energy. Performing the additional modelling and difference phase allows a more effective suppression of the converted wave energy in the data domain.

Examples

Case study 1 – Egypt

The first case study comes from Egyptian waters in the eastern Mediterranean Sea. Seismic processing was performed on an area of approximately 4700 km², and comprised data from five separate acquisition surveys. The main contributing dataset to the seismic volume was acquired in 2017 by the PGS vessel M/V Ramform Tethys. The survey was acquired with a configuration using 14 dual-sensor streamers, each 9000-m long, towed at a depth of 25 m and with a total surface spread width covering 1300 m. Two source arrays were used shooting at 25 m flip to flop. The nominal seismic acquisition bin size was 6.25 m by 25 m, with 80 fold of coverage.

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subsurface stack after the application of the converted wave attenuation workflow. The green arrows in Figure 6b point to the same location as the red arrows in Figure 6a. It is evident that the described workflow has successfully attenuated the converted wave energy. Figure 7 shows the result of the workflow in the data domain on common shot gathers. Converted waves are harder to identify in the shot records. However, it can be traced easily from the stack dataset. Arrows indicate where the recorded converted wave energy resides in the shot gathers. Again, it is clear that the converted wave energy has been attenuated by the proposed workflow.

Figures 8 and 9 show the results of the methodology in the image domain obtained by migrating data using a Kirchhoff algorithm. Figures 8a and 8b show the result on common depth point (CDP) gathers, where the converted wave has been marked with arrows. The move-out of this energy is quite small, approximately 100 ms at 8 km offset, making it difficult to filter using normal move-out based methods. Figures 9a and 9b show the same data after stacking. The effectiveness of the flow in attenuating recorded converted wave energy, which acts as noise in the P-wave image, is self-evident. Figure 9c illustrates the difference of the application, showing the attenuated energy and its response to the migration operator.

**Case study 2 – Cyprus**

Data for the second case study were acquired for PGS MultiClient in Block 10 offshore Cyprus by PGS vessels M/V Ramform Tethys and Hyperion, commencing in 2016 and completing in 2017. The total area acquired was 6045 km². The data were acquired using a spread of 14 dual-sensor streamers each 9000-m long and separated by 100 m. Two sources were used with a 25 m flip to flop shooting interval.

The velocity model for the modelling was generated using tomography in the post-salt section to estimate the sediment velocity. During the velocity analysis for the salt bodies, it was observed that there were regions of dirty salt, requiring a slower average salt velocity than areas of clean salt. A spatially variable salt velocity was inserted with a background clean salt velocity of 4350 m/s, and slower velocities, in the regions containing dirty salt such that the gather flatness at the base salt, were optimized.

![Figure 10](image)

*Figure 10* Raw shot gather showing the mode converted energy lying beneath the base salt reflector (a); raw shot gather with asymmetrical mode conversion model overlain (b) and shot gather after converted energy removed (c).

![Figure 11](image)

*Figure 11* Depth migrated CDP gathers from before (a) and after (b) the mode conversion removal. The location of the mode converted energy is highlighted by the red arrows. Once the energy is removed the weaker amplitude primary events become more visible.
Using equations (1) and (2), the analysis of the depth of the converted energy below the salt versus salt thickness suggested that a \( V_p/V_s \) ratio of 1.8 was appropriate in this area; the S-wave salt velocity model used for the modelling was a scaled version of P-wave model in the salt.

Figure 10 shows a common shot gather from the survey area annotated with the location of the asymmetrical mode converted energy, and results after the mode converted energy has been removed. The effectiveness of the converted energy removal is clearly visible in the pre-stack data domain gathers. Figure 12 shows Kirchhoff depth stack images before and after the removal of the mode converted energy. As with the example from Egypt, the ‘ghost’ reflector under the salt is attenuated. This results in a cleaner pre-salt image, where primary P-wave energy dipping up against the base salt is revealed, and data interpretability is significantly improved, particularly as the base salt can form a trap to prospectivity in this area. The pre-stack data in Figure 11 also shows the elimination of the low-frequency converted wave energy. Attribute analysis on this data is contaminated by the noise from the mode transformation, where amplitudes analysis shows an inconsistent behaviour if the noise is not attenuated.

**Conclusions**

Converted wave energy following either asymmetrical (PSPP, PPSP) or symmetrical (PSSP) modes can significantly hinder data usage, particularly in salt provinces such as the eastern Mediterranean Sea, where prospectivity exists in the pre-salt section. We have demonstrated, in two distinct locations, a simple but effective approach that attenuates the offending noise, revealing the pre-salt reflectivity, and reducing risk associated with both data interpretability and attributes analysis.

**Acknowledgements**

The authors wish to thank PGS MultiClient for authorization to show examples from the different surveys acquired by PGS throughout the eastern Mediterranean. We would like to give special thanks to all the geophysicists from PGS who helped us in producing the results.

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